

Single Mode Optical Fiber - Dispersion

1 OBJECTIVE

Characterize analytically and through simulation the effects of dispersion on optical systems.

2 PRE-LAB

A single mode fiber, as the name implies, supports only a single transverse mode. The benefits of supporting only a single mode is that modal dispersion is eliminated since all pulses travel with the same modal group velocity. The fundamental mode of optical fibers is shown below in figure 1. For a core/cladding fiber structure the field follows a Bessel function, which can be approximated quite well by a Gaussian field for weakly guiding structures.

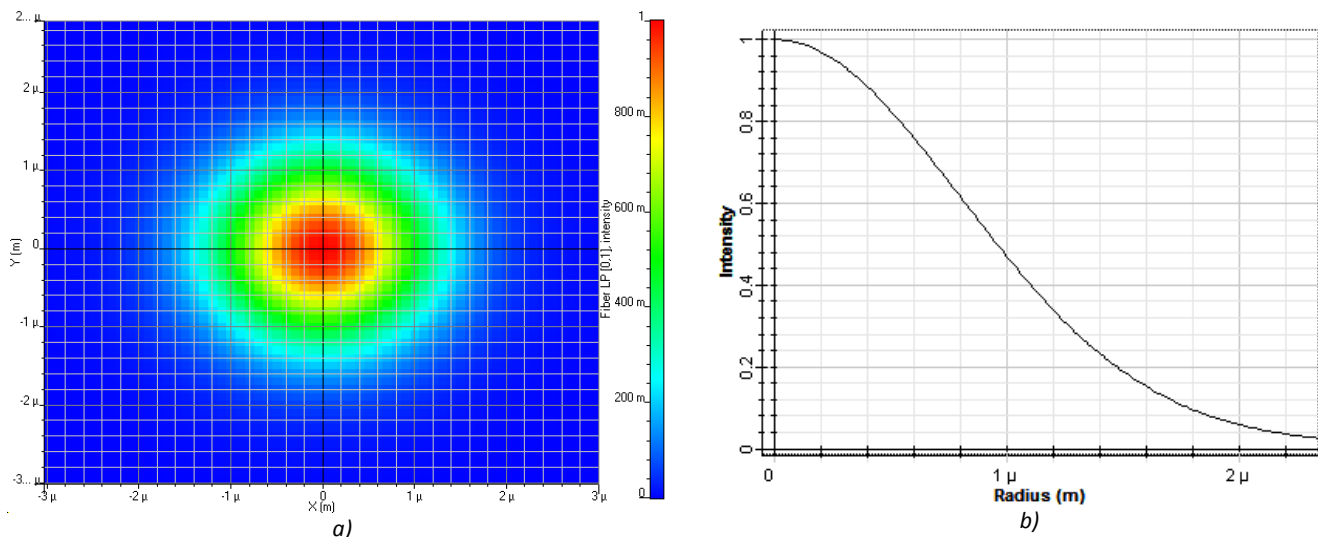


Figure 1: The fundamental mode of a single mode fiber: a) The intensity profile in the traverse direction. b) Intensity as a function of radius.

Questions:

- 2.1 How many orthogonal modes exist in a single mode fiber? Hint: Consider the rotational symmetry of the fiber and vector field attributes of the electric field.

Answer: There are actually two orthogonal modes. Both with the same spatial intensity, but their main electric field component offset by 90 degrees. It is possible to have an E_x and E_y polarized mode.

2.1 CHROMATIC DISPERSION

Although there is no modal dispersion between different propagating modes, dispersion has not been completely eliminated. For a single mode fiber, the dominant forms of dispersion are material and waveguide dispersion. Material dispersion stems from the frequency dependence of the index of refraction, whereas the waveguide dispersion arises from the frequency dependence of the propagation constant for the fundamental mode. Together these two related effects force a frequency dependence for the group velocity of a pulse.

If the derivative of the group velocity with respect to the frequency, $v_g = \frac{d\omega}{d\beta}$, is non-zero then a time pulse will broaden through propagation as the different spectral components will arrive at different times. The pulse broadening, ΔT , is related to the derivative of the phase constant, β by:

$$\Delta T = L \frac{d^2\beta}{d\omega^2} \Delta\omega = L\beta_2 \Delta\omega, \quad (1)$$

where $\Delta\omega$ is the spectral width of the pulse. In another form the pulse broadening can be given in terms of the wavelength range:

$$\Delta T = LD\Delta\lambda, \quad (2)$$

where D is called the dispersion parameter.

$$D = -\frac{2\pi c}{\lambda^2} \beta_2 \quad (3)$$

If a fiber has a positive dispersion parameter it is called anomalous dispersion and higher frequency components travel faster. If the dispersion parameter is negative it is called normal dispersion and lower frequency components travel faster.

Below is an example of a dispersion broadened pulse, notice that in addition to the pulse width increasing, so does the peak power decrease.

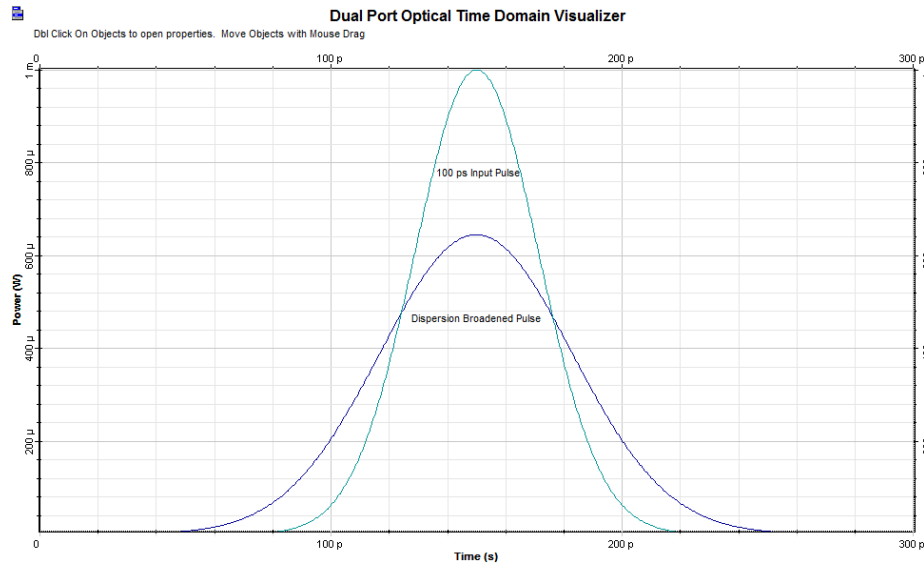


Figure 2: Dispersion Broadening of a 100 ps time pulse after 50 km propagation through an anomalous dispersive fiber.

Dispersion is quite simple to model by itself. In fact, its effect on a pulse can be modelled by the differential equation:

$$\frac{\partial A}{\partial z} + \frac{i\beta_2}{2} \frac{\partial^2 A}{\partial t^2} - \frac{\beta_3}{6} \frac{\partial^3 A}{\partial t^3} = 0. \quad (4)$$

This equation is set in the reference frame of the moving pulse with pulse shape $A(z, t)$. The higher order dispersion term β_3 is ignored for now, which makes solving the equation much simpler.

Questions:

- 2.1.1 Calculate the time delay after 50 km of propagation between two frequency components separated by 2 nm and with a dispersion parameter of 16.75 ps/km · nm

Answer: $\Delta T = LD\Delta\lambda = 50 * 16.75 * 2 = 1675 \text{ ps}$

- 2.1.2 Derive an expression for $\Delta\omega$ as a function of $\Delta\lambda$ using $c = \frac{\omega}{2\pi} \lambda$.

Answer:

$$c = \frac{\omega}{2\pi} \lambda$$

$$\omega = \frac{2\pi}{\lambda} c$$

$$\frac{\Delta\omega}{\Delta\lambda} = -\frac{2\pi}{\lambda^2} c$$

$$\Delta\omega = -\frac{2\pi}{\lambda^2} c \Delta\lambda$$

- 2.1.3 For an optical pulse of constant phase propagating in a normal dispersion fiber. Which frequency components will be detected first to at the leading edge of the pulse?

Answer: The lower frequency components will travel faster and move towards the leading edge of the pulse.

2.2 CHIRPING OF PULSES

Optical signals can be represented by complex envelopes modulated at a carrier frequency, ω . That is to say, the optical pulses can be represented mathematically as:

$$E_x(t) = |A(t)|e^{j\varphi(t)}e^{j\omega t}, \quad (5)$$

where $A(t)$ is a complex valued function and:

$$\varphi(t) = \arg[A(t)]. \quad (6)$$

A simple Gaussian pulse would be of the form:

$$E_x(t) = e^{-(t)^2}e^{j\omega t}. \quad (7)$$

Below is an example of what the magnitude and real part of these functions would look like. The $\varphi(t)$ value is constant 0 for this signal. The real part of the signal would be the actual electric field value, but representing the field as an envelope and removing the explicit representation of the carrier frequency is a useful tool, for example in the description of chromatic dispersion in the previous chapter.

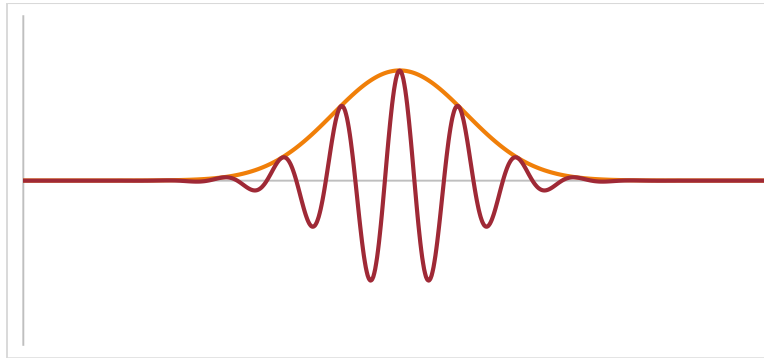


Figure 3: Gaussian pulse envelope with the real part of the signal shown as well.

Instead of a purely real Gaussian pulse, we will introduce a time dependent phase $\varphi(t)$. This will be represented by the equation:

$$E_x(t) = e^{-(t)^2}e^{jCt^2}e^{j\omega t}. \quad (8)$$

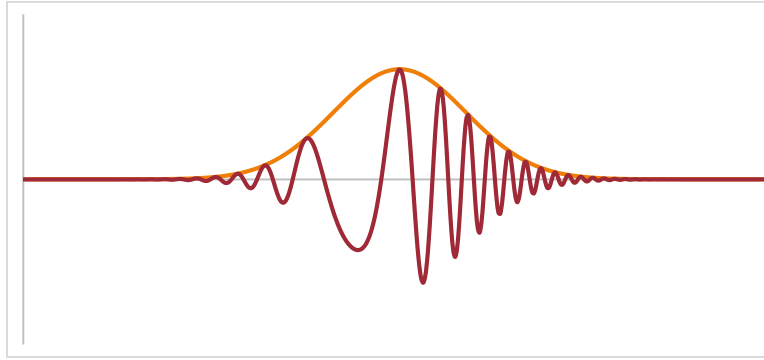


Figure 4: A chirped Gaussian envelope clearly showing the change in the carrier frequency as the phase changes over the pulse.

This effect is known as chirp, described by the constant C , the chirp parameter. This time dependent phase results in a linear change in the instantaneous frequency. Changing the phase of the envelope has no effect on the magnitude of the original envelope, but it does change the frequency content.

Questions:

- 2.1.1 From the expression for the simple chirped Gaussian pulse, find the instantaneous frequency $\omega(t)$ which can be derived from the derivative of the phase with respect to time.

Answer: $E_x(t) = e^{-(t)^2} e^{jCt^2} e^{j\omega t}$

$$\omega_i(t) = \frac{d}{dt} (Ct^2 + \omega t)$$

$$\omega_i(t) = 2Ct + \omega$$

3 EFFECT OF DISPERSION ON PULSES

Short pulses in optical fiber are broadened by group velocity dispersion. Naturally in OptiSystem it is possible to simulate these effects on pulses. Setting up a layout, as in the example below the effects can be investigated in more detail.

3.1 BROADENING OF GAUSSIAN PULSES

Only a few changes to the default parameters is needed to begin the simulation. Place a User Defined Bit Sequence Generator, setting the bit sequence to "0100000000000000" and the Sequence length in the Layout parameters to 16 bits. This allows for the injection of a single pulse. In the Optical Fiber disable the Attenuation effect, Third-order Dispersion and Self-phase modulation. In the PMD tab, set the Birefringence type to "Deterministic" and set Differential group delay to 0. This creates an optical fiber model that only includes group velocity dispersion. For an increase in simulation accuracy setting the Samples per bit to 256 will be large enough to provide very accurate simulations while keep the simulation time low.

- User Defined Bit Sequence Generator Transmitters Library/Bit Sequence Generators

- Optical Gaussian Pulse Generator
 - Fork 1x2
 - Optical Power Detector
 - Time Delay
 - Clock Recovery
 - Optical Time Domain Visualizer
 - Optical Spectrum Analyzer
 - Dual Port Optical Time Domain Visualizer
 - Dual Port Optical Spectrum Analyzer
- Transmitters Library/Pulse Generators/Optical
 - Tools Library
 - Receivers Library/Photodetectors
 - Passives Library/Optical
 - Receivers Library/Regenerators
 - Visualizer Library/Optical
 - Visualizer Library/Optical
 - Visualizer Library/Compare
 - Visualizer Library/Compare

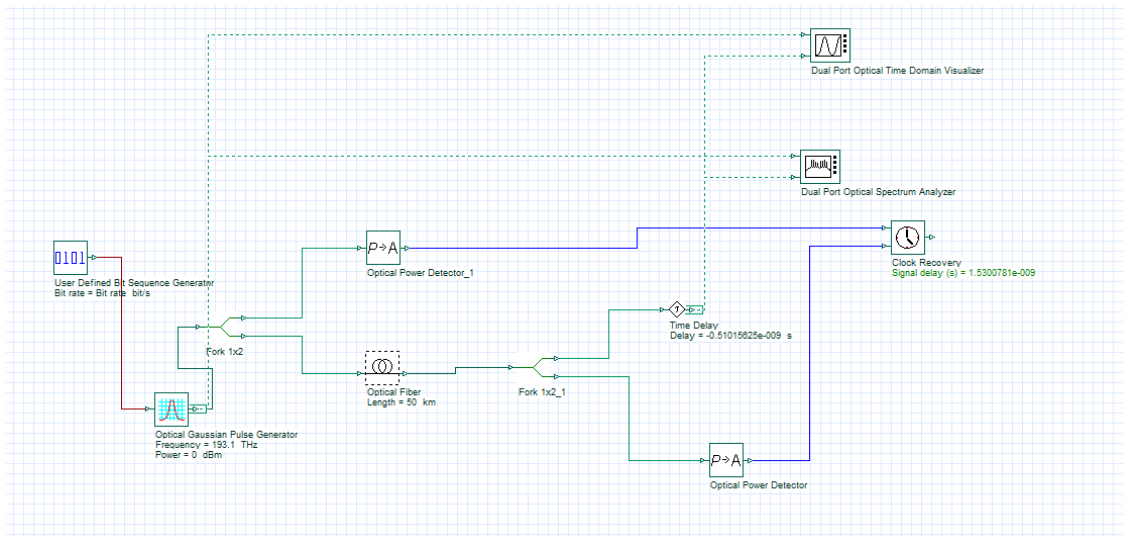


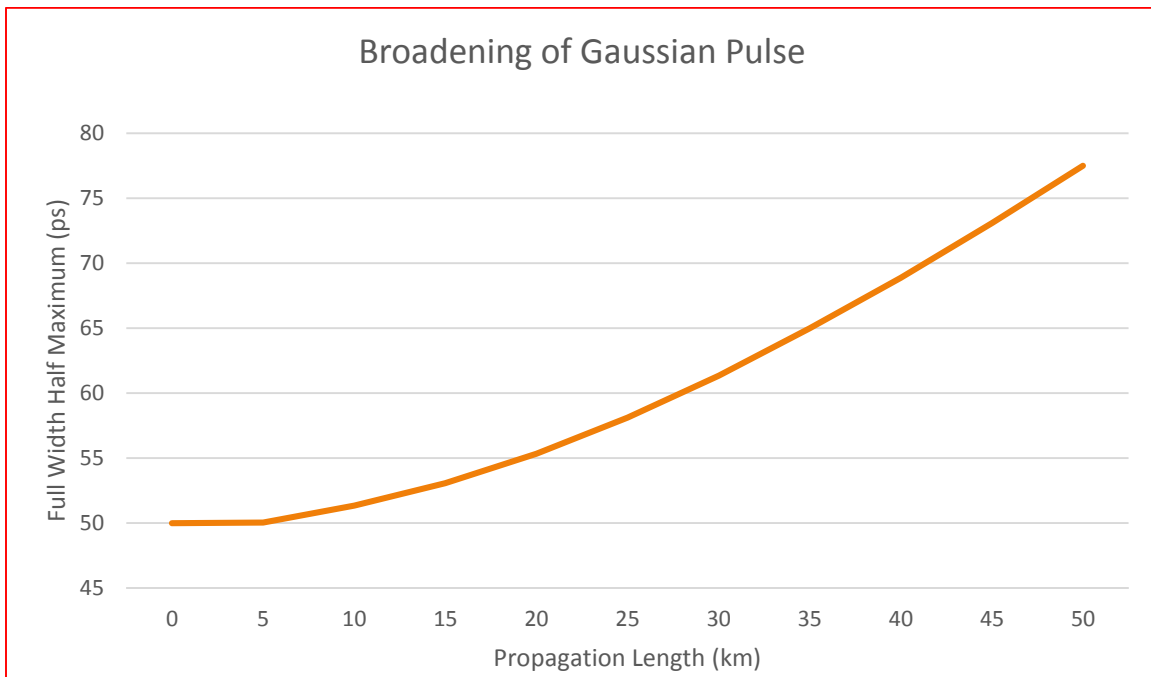
Figure 5: Layout for simulating dispersion.

The group velocity dispersion will also cause a slight delay to the entire envelope in relation to the input pulse, so the Clock Recovery component is used in conjunction with the Time Delay component to re-center the pulse with the input. Using markers in the time domain graph it is straightforward to calculate the FWHM of the pulses.

Questions:

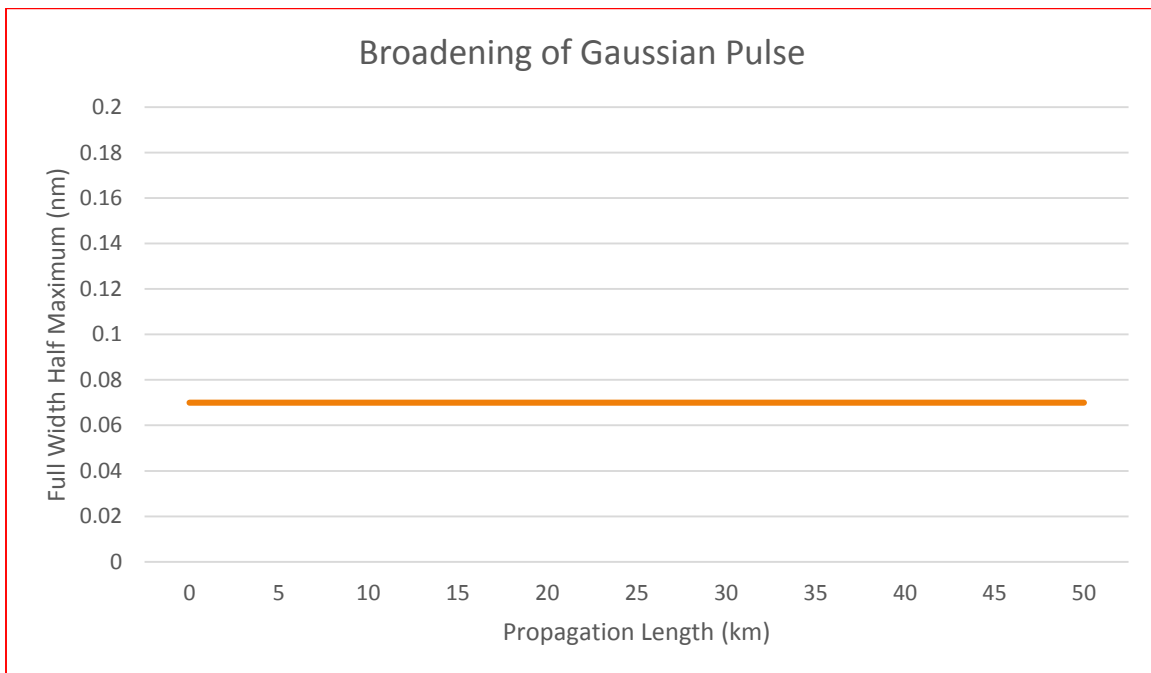
- 3.1.1 Using this setup and the default setting for group velocity dispersion, plot the T_{FWHM} as a function of distance. Describe the relation.

Answer: The pulse broadens linearly for large distances



3.1.2 Using this setup and the default setting for group velocity dispersion, plot the ω_{FWHM} as a function of distance. Describe the relation.

Answer: There is no change to the spectrum or spectral width of the pulse as a function of distance.



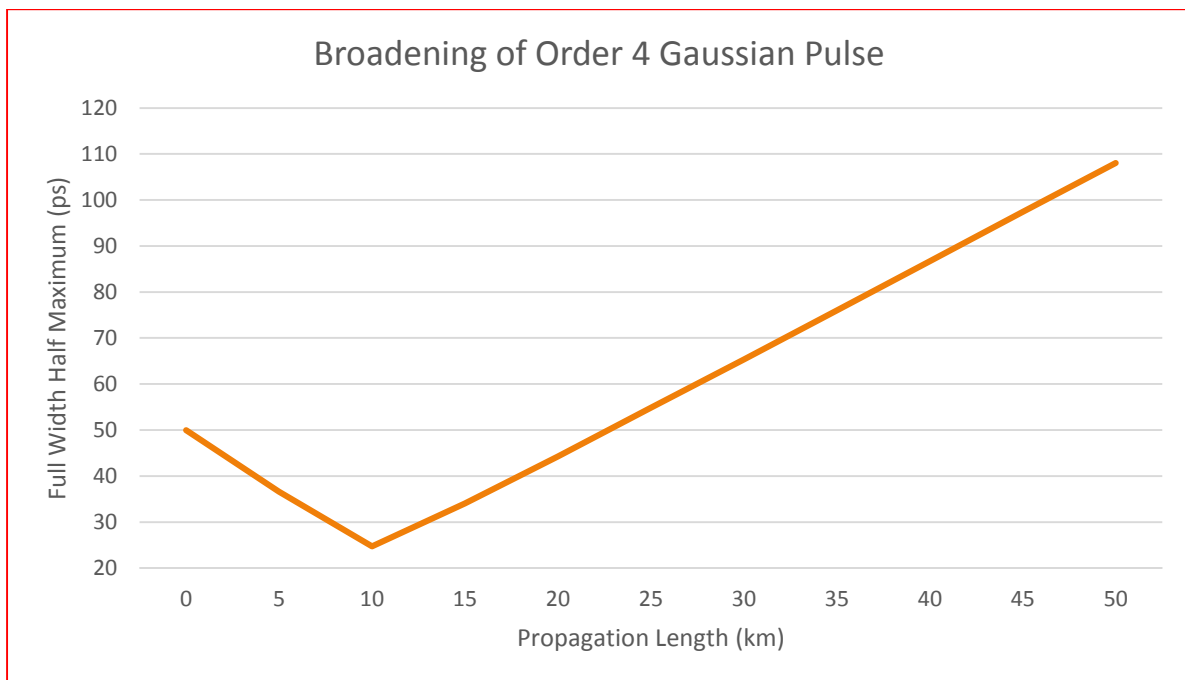
3.1.3 Does dispersion modify the magnitudes of the frequency components? Does it affect the phase or time delay of the frequency components?

Answer: Dispersion has zero effect on the magnitudes of the frequency components, however the phase does change. Plotting the real and imaginary parts of the spectral components would show a change.

3.2 BROADENING OF HIGHER ORDER GAUSSIAN PULSES

3.3.1 Change the order of the Gaussian pulse to 4 and plot the T_{FWHM} as a function of distance. Describe the relation.

Answer: The pulse broadens linearly for large distances and at first compresses. The full width half maximum spreads much quicker than the first order Gaussian.



3.3.2 Explain the strange behavior of the full width half maximum for short distances. Is the T_{FWHM} the best method for measuring spreading? Compared to the first order Gaussian the fourth order spreads much more quickly, by comparing the spectrums of both explain why.

Answer: The T_{FWHM} gets smaller for short distances because two pulses spread out from the main pulse and the center pulses gets shorter and thinner, which artificially cause the smaller T_{FWHM} . For comparing pulses of the same type T_{FWHM} is good enough, but for different pulses especially for ones with smaller side lobes there are better techniques for measuring dispersion.

The spectrum is larger for the higher order Gaussian, therefore there is a larger difference in group velocities for the smallest and largest frequency component. Thus dispersion effects it more. The same is generally true for any shorter pulse.

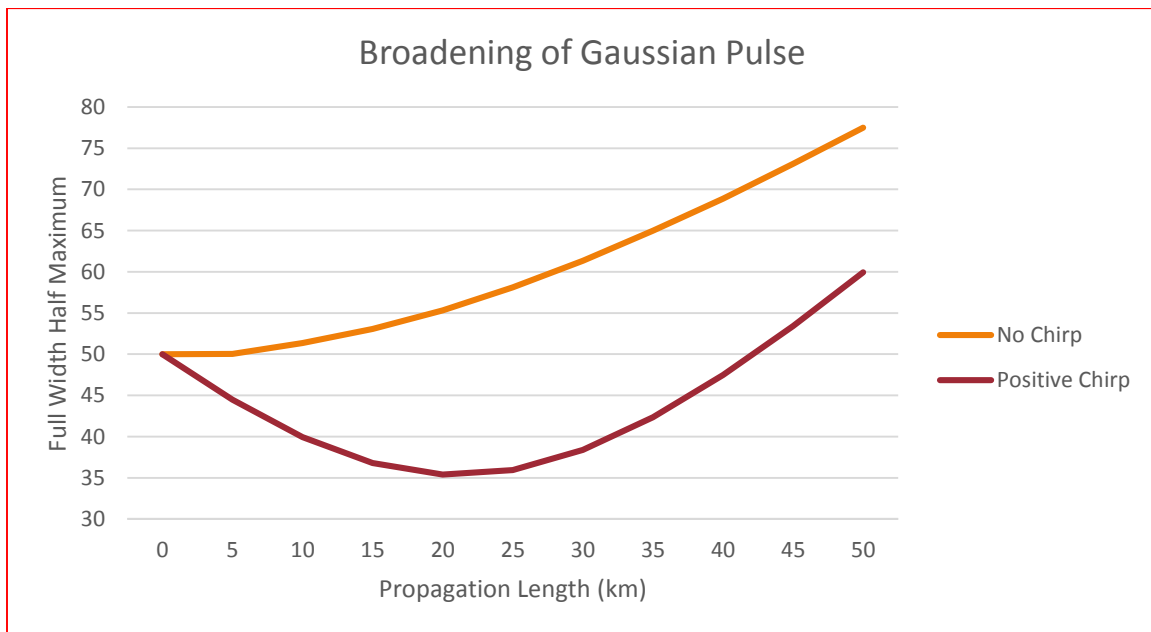
3.3 BROADENING OF CHIRPED GAUSSIAN PULSES

The chirp parameter for a Gaussian pulse of pulse width $T_0 \approx T_{FWHM}/1.665$ is defined as the rate of change of the instantaneous frequency multiplied by T_0^2 with the equation for the instantaneous frequency being:

$$\delta\omega = \frac{c}{T_0^2} t. \quad (9)$$

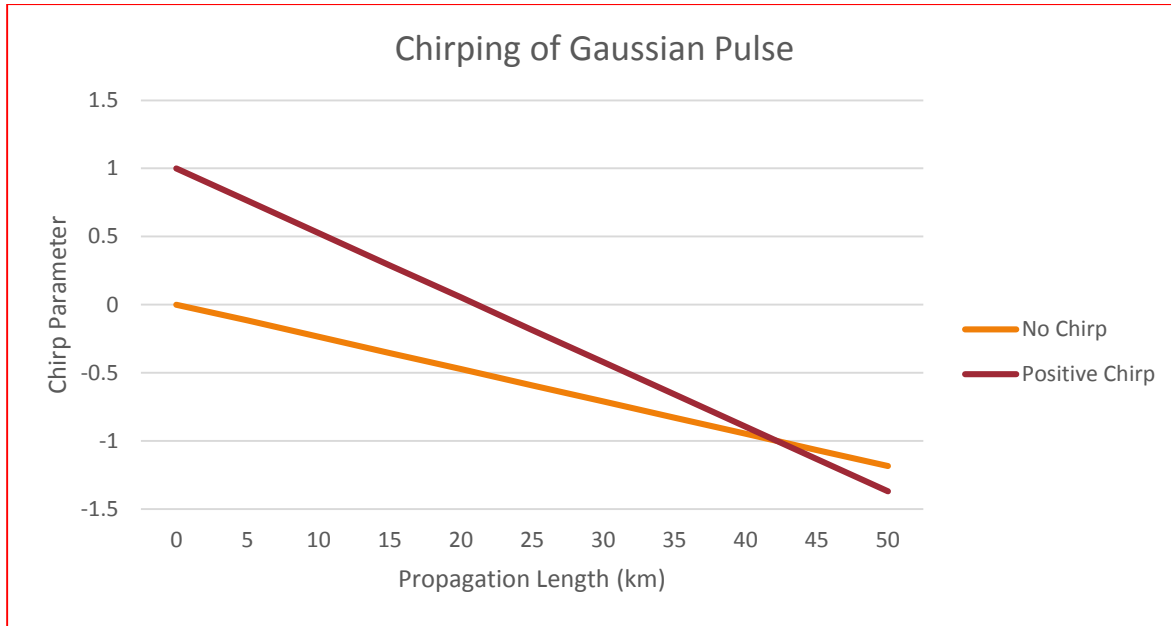
- 3.3.3 Plot T_{FWHM} for a regular and chirped Gaussian pulse as a function of distance. In the Optical Gaussian Pulse Generator set the Chirp factor in the Chirp tab to 1 rad/s. Describe the difference.

Answer: The pulse broadens linearly for large distances and at first compresses. The full width half maximum spreads faster after the initial compression, than the Gaussian pulse with no chirp.



- 3.3.4 Plot the chirp for a regular and chirped Gaussian pulse as a function of distance. In the Optical Gaussian Pulse Generator set the Chirp factor in the Chirp tab to 1 rad/s. Describe the difference.

Answer: The chirp decreases linearly with distance as the fiber causes anomalous dispersion. The chirped pulse has a larger slope than the normal Gaussian pulse.



4 REPORT

In your lab report include the following:

- Brief overview of the background and theory.
- Answers to all pre lab questions, clearly showing your work.
- Brief description of the simulation method and setup, including screenshots.
- Final results including figures and discussion.

5 REFERENCES

- [1] Agrawal, G. P. *Fiber-optic Communication Systems*. New York: Wiley, 1997. Print.
- [2] Saleh, Bahaa E. A., and Malvin Carl. Teich. *Fundamentals of Photonics*. New York: Wiley, 1991. Print.